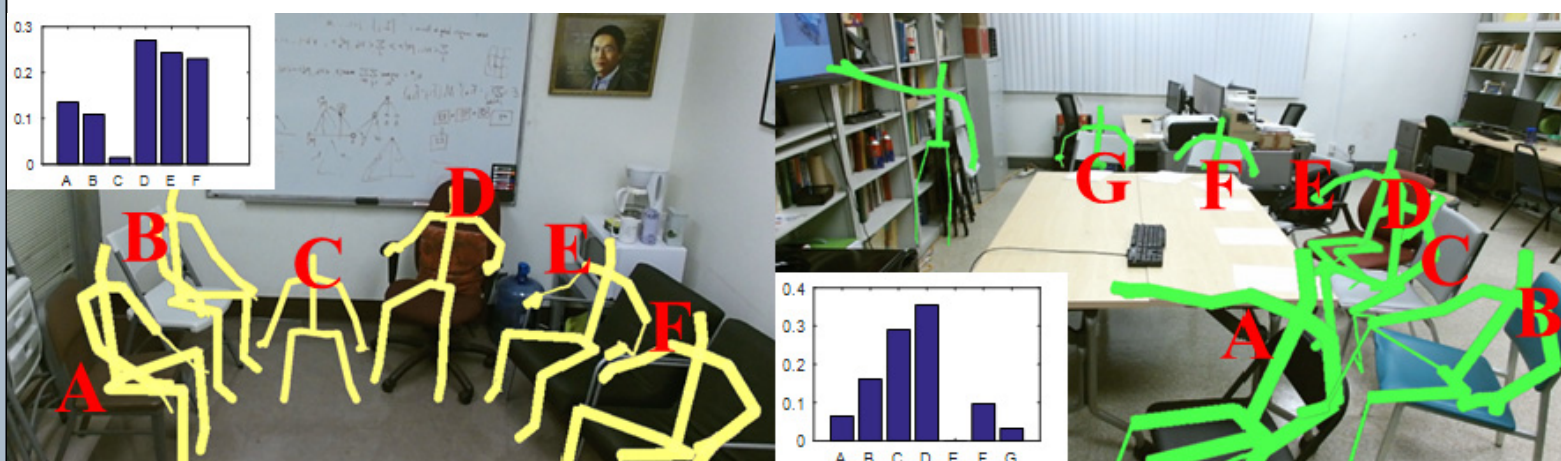
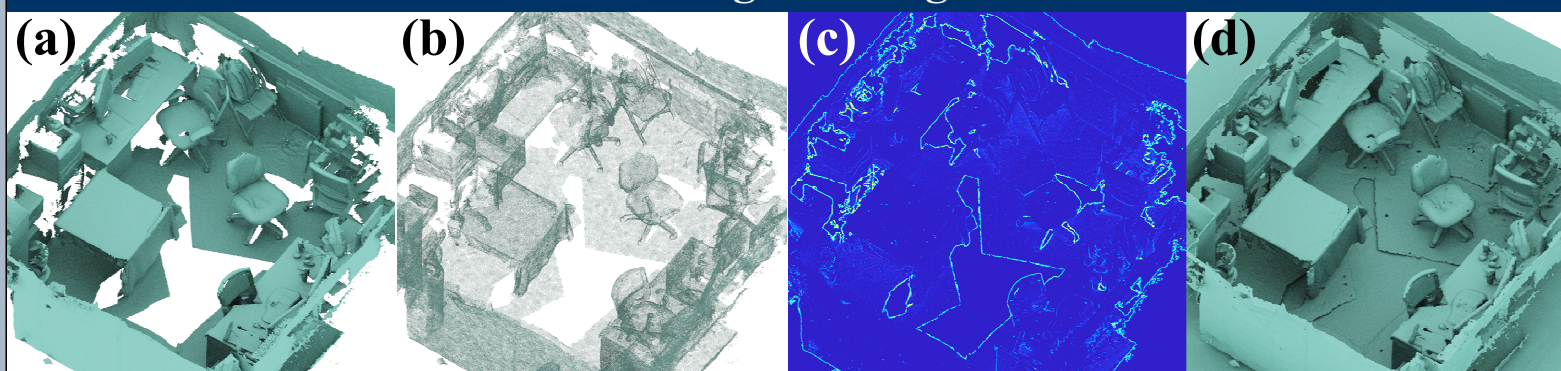


## Motivation

We propose a notion of affordance that takes into account **physical quantities** generated when the human body interacts with real-world objects, and introduce a learning framework that incorporates the concept of **human utilities**, which in our opinion provides a deeper and finer-grained account not only of object affordance but also of people’s interaction with objects.



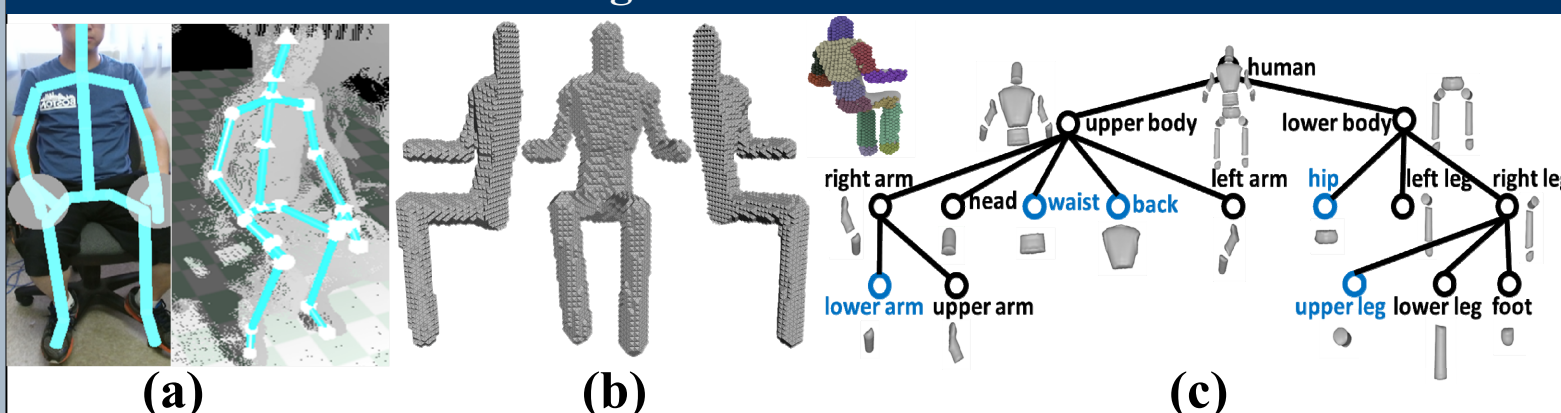
## Reconstructing Watertight Scenes



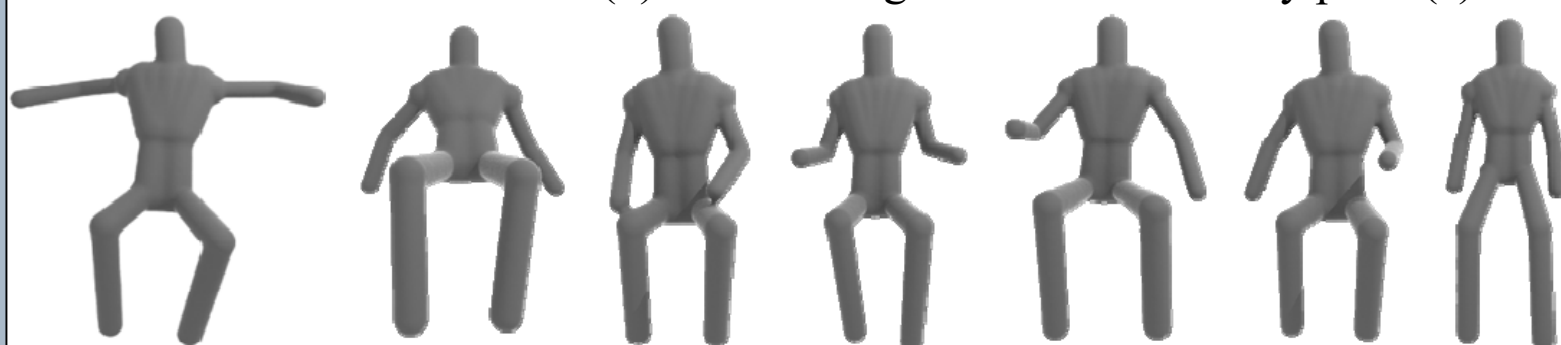
From a reconstructed 3D indoor scene (a), we uniformly sample vertices in the input mesh with Poisson disk sampling (b), then convert them into a watertight mesh (d) with well-defined interior and exterior regions. Differences (c) between the input mesh and the converted watertight mesh.



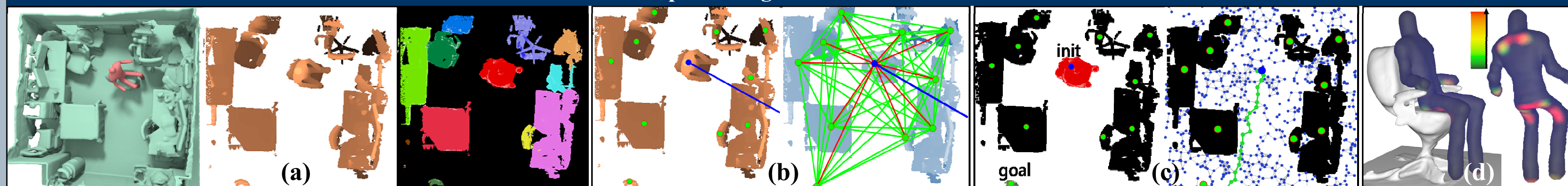
## Modeling Volumetric Human Pose



The stick-man model (a) captured using a Kinect is converted into a tetrahedralized human model (b) and then segmented into 14 body parts (c).



## Data Pre-processing and Feature Extractions



**(a) Data pre-processing.** Given a reconstructed 3D scene, we project it down onto a planar map, and segment 3D objects from the scene.

**(b) Spatial Entities and Relations in 3D Spaces.** Visualization of 3D object positions (green dots), human head position (blue dot), and orientation (blue line). Spatial features  $\phi_i(\mathbf{G})$  are defined as human-object (red lines) and object-object (green lines) relative distances and orientations.

(c) **Human Utilities in Time.** Temporal features  $\phi_t(G)$  are defined as the plan cost from a given initial position to a goal position.

(d) **Physical Quantities of Human Utilities.** Using FEM simulation, the physical quantities  $\phi_n$  (G) are estimated at each vertex of the FEM mesh.

## Simulating Human Interactions with Scenes

We used **Finite Element Method** to simulate human tissue dynamics.

**Input:** reconstructed watertight scenes and volumetric human poses.

**Outputs:** forces and pressures.

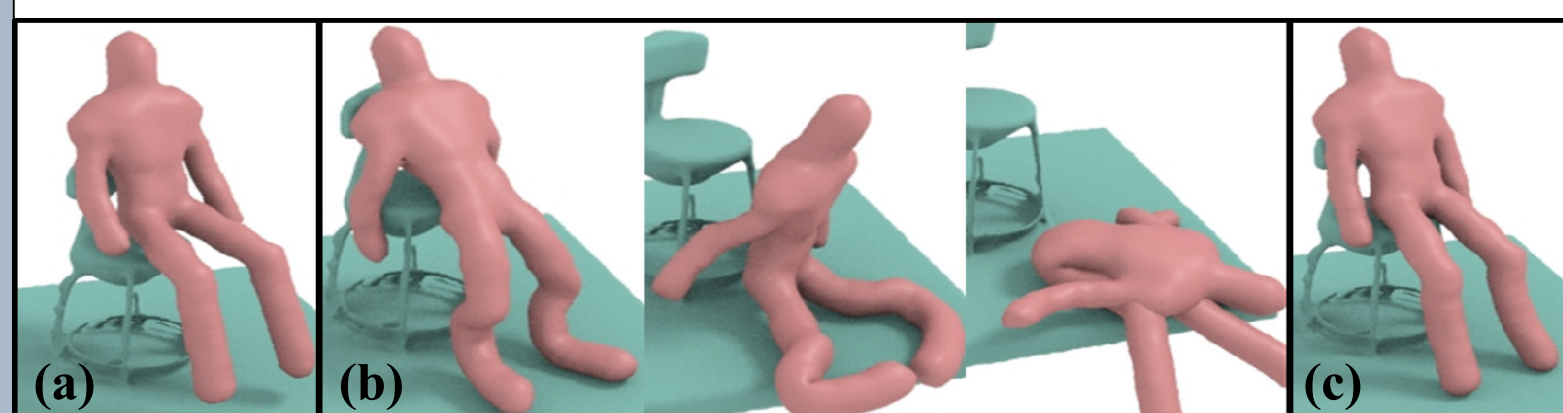
Timestep: $1 \times 10^{-3}s$	Density: $1000kg/m^3$	Young's modulus: $0.15kPa$	Poisson's ratio: 0.3
Collision stiffness: $1 \times 10^4 kg/s^2$	Friction coeff: $1 \times 10^{-3}$	Damping coeff: $50kg/s$	Gravity: $9.81m/s^2$

**Elasticity:** The human body is modeled as an elastic material. The total elastic potential energy is defined as:  $\Phi^E(\mathbf{x}) = \int_O \Psi^E(\mathbf{x}) d\mathbf{x} \approx \sum_e V_e^0 \Psi^E(\mathbf{F}(\mathbf{x}))$ .

**Contact forces:** To model contact forces, we need to penalize penetrations of the human body mesh into the scene mesh. If a penetration is detected for vertex  $i$ , a collision energy that penalizes the penetration distance in the normal direction is assigned to the corresponding vertex:  $\Phi^C(\mathbf{x}_i) = \frac{1}{2}k_c(\mathbf{x}_i - \mathcal{P}(\mathbf{x}_i))^2$ .

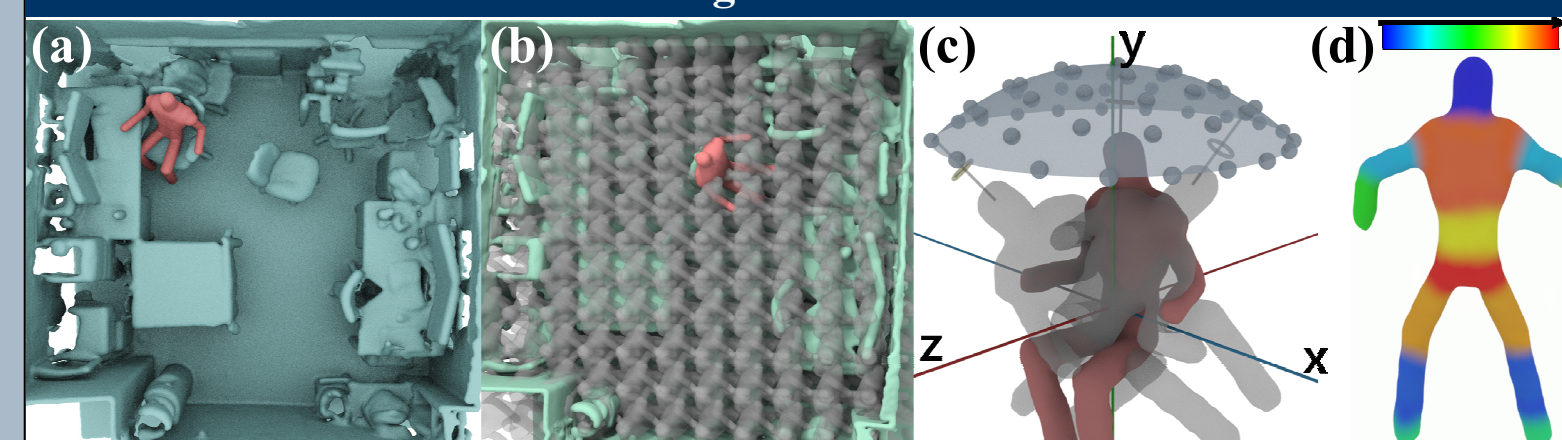
**Dynamics integration:** Backward Euler time integration is used to solve the momentum equation. From time  $n$  to  $n + 1$ , the nonlinear system to solve is:

$$\begin{aligned} \mathbf{M} \frac{\mathbf{v}^{n+1} - \mathbf{v}^n}{\Delta t} &= \mathbf{f}(\mathbf{x}^{n+1}, \mathbf{v}^{n+1}) + \mathbf{M}g, \\ \mathbf{f}(\mathbf{x}^{n+1}, \mathbf{v}^{n+1}) &= \mathbf{f}^E(\mathbf{x}^{n+1}) + \mathbf{f}^C(\mathbf{x}^{n+1}) + \mathbf{f}^D(\mathbf{v}^{n+1}), \\ \mathbf{x}^{n+1} - \mathbf{x}^n &= \mathbf{v}^{n+1} \Delta t. \end{aligned}$$

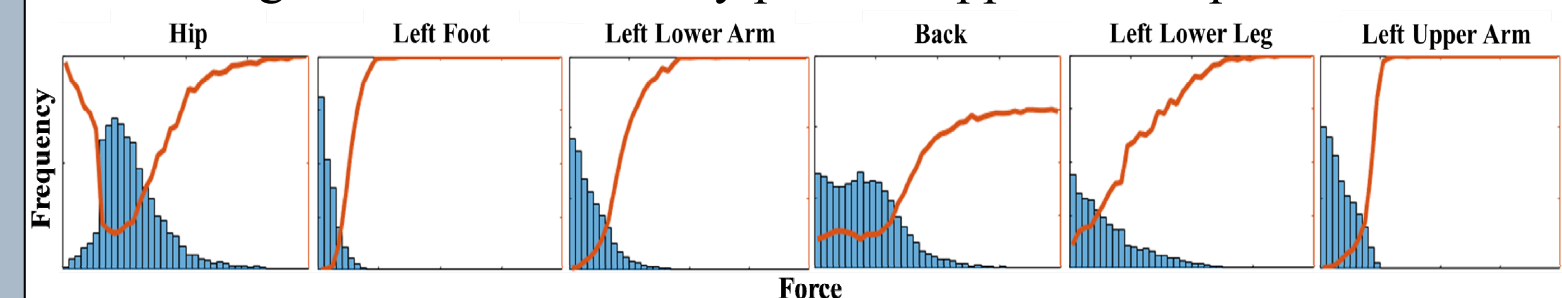


Given an initial human pose in a 3D scene subject to gravity (a), without adequate damping (b) the human body is too energetic and produces unnaturally bouncy motion. With proper damping, the simulation converges to a physically stable rest pose (c) in a small number of timesteps.

## Learning Human Utilities



(a) We assume that the observed demonstration is near-optimal, and therefore regard it a positive example. The learning algorithm then imagines different configurations by initializing with different human poses  $P_a$ , (b) translations  $T_b$ , and (c) orientations  $O_c$ . The imagined randomly generated configurations are regarded negative examples. (d) The average forces of each body part remapped to a T pose.



**Learning** the ranking function is equivalent to finding the coefficient vector such that the maximum number of the inequalities are satisfied:

$$\langle \omega, \phi(\mathcal{G}^*) \rangle > \langle \omega, \phi(\mathcal{G}_i) \rangle, \quad \forall i \in \{1, 2, \dots, n\}$$

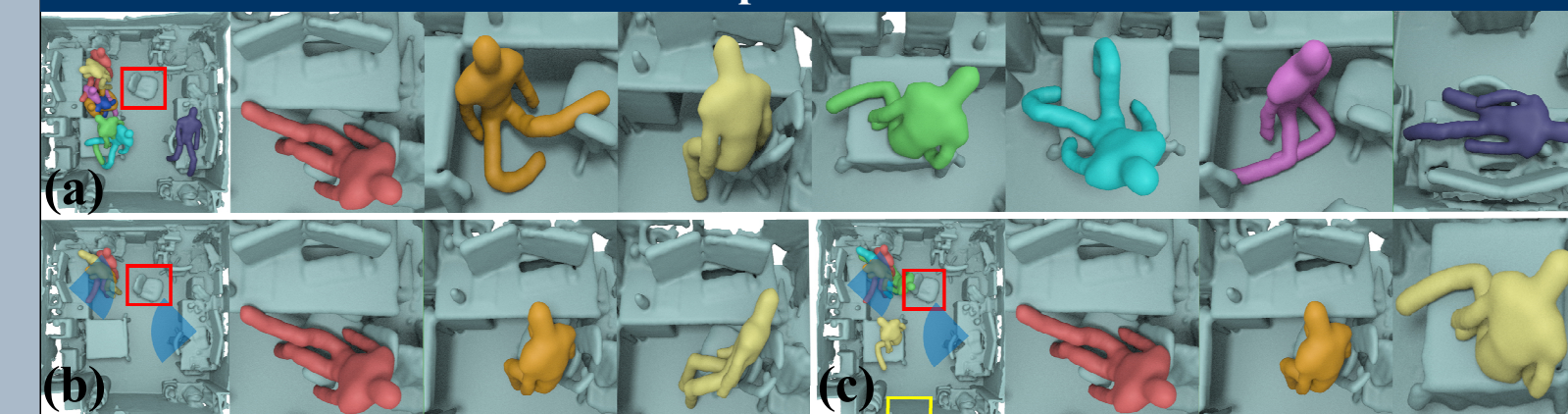
To approximate the solution, we introduce non-negative slack variables

$$\begin{aligned} & \min \frac{1}{2} \langle \omega, \omega \rangle + \lambda \sum_i^n \xi_i^2, \quad \forall i \in \{1, \dots, n\} \\ & \text{s.t. } \xi_i > 0, \quad \langle \omega, \phi(\mathcal{G}^*) \rangle - \langle \omega, \phi(\mathcal{G}_i) \rangle > 1. \end{aligned}$$

In the **inference** phase, the goal is to find, among all the imagined configurations in the solution space, the best configuration that receives the highest score:

$$\mathcal{G}^* = \arg \max_{\mathcal{G}_i} \langle \omega, \phi(\mathcal{G}_i) \rangle$$

## Experiments



(a) The top 7 human poses using physical quantities. The algorithm seeks physically comfortable sitting poses, resulting in casual sitting styles; e.g., lying on the desk. (b) Improved results after adding spatial features to restrict the human-object relative orientations and distances. Further including temporal features yields the most natural poses (c).

